

Digital Image Processing

Image Enhancement
(Histogram Processing)

Over the next few lectures we will look at image enhancement techniques working in the spatial domain:

- What is image enhancement?
- Different kinds of image enhancement
- Histogram processing
- Point processing
- Neighbourhood operations

A Note About Grey Levels

So far when we have spoken about image grey level values we have said they are in the range $[0, 255]$

- Where 0 is black and 255 is white

There is no reason why we have to use this range

- The range $[0,255]$ stems from display technologies

For many of the image processing operations in this lecture grey levels are assumed to be given in the range $[0.0, 1.0]$

What Is Image Enhancement?

Image enhancement is the process of making images more useful.

The reasons for doing this include:

- Highlighting interesting detail in images,
- Removing noise from images,
- Making images more visually appealing.

Image Enhancement Examples



Image Enhancement Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

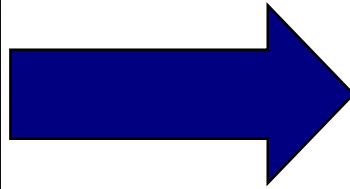
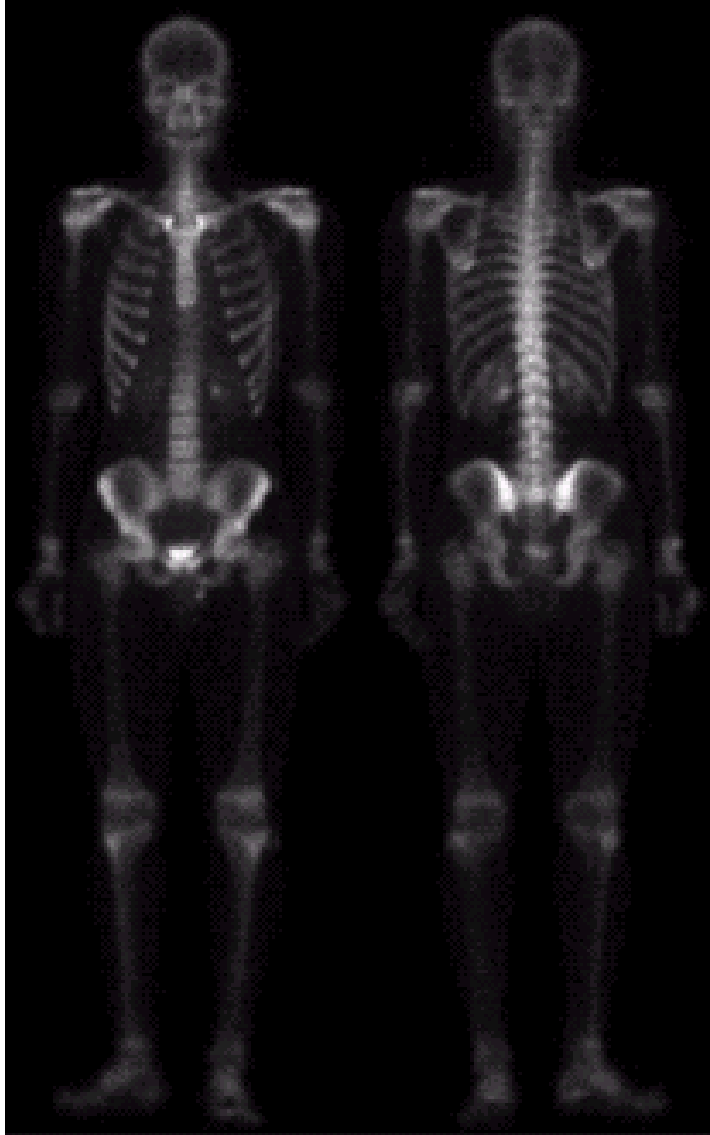


Image Enhancement Examples (cont...)

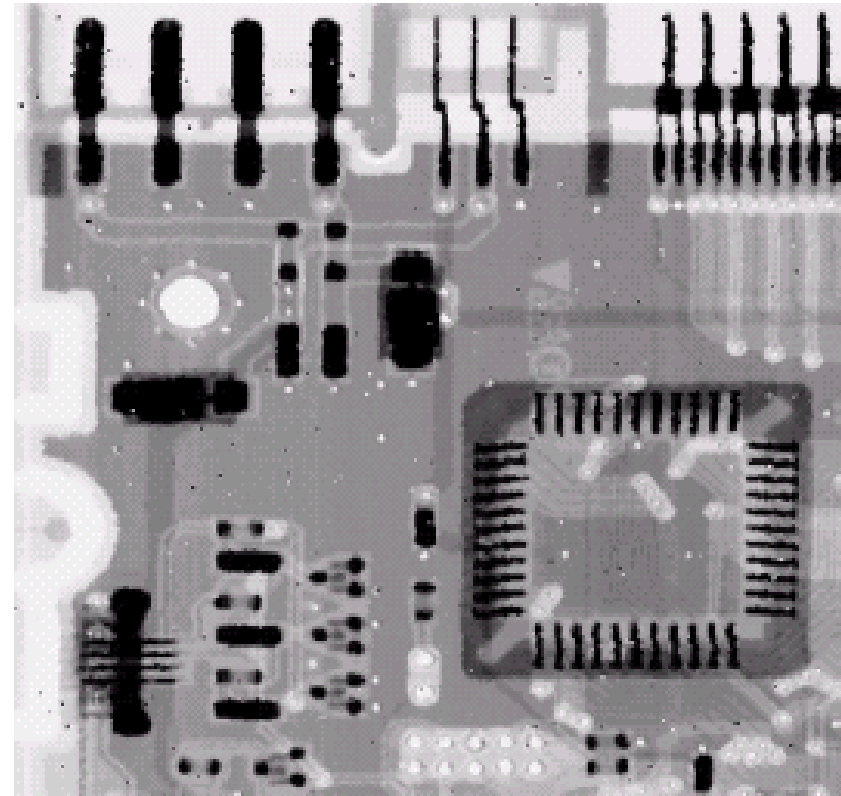
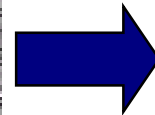
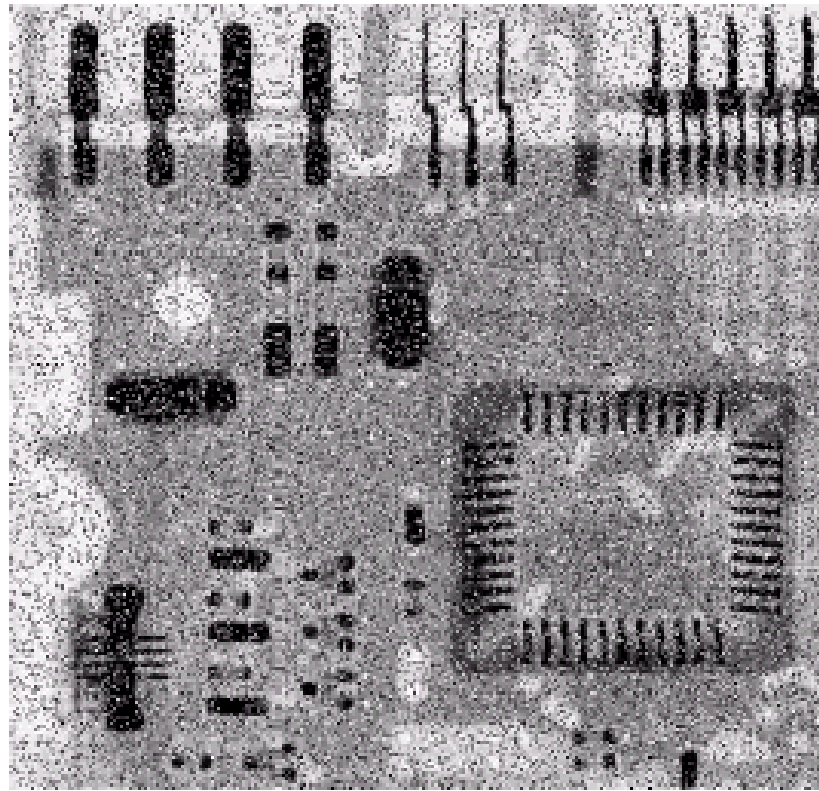
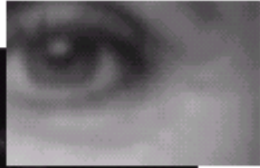


Image Enhancement Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



Spatial & Frequency Domains

There are two broad categories of image enhancement techniques

- Spatial domain techniques
 - Direct manipulation of image pixels
- Frequency domain techniques
 - Manipulation of Fourier transform or wavelet transform of an image

For the moment we will concentrate on techniques that operate in the spatial domain.

The histogram of an image shows us the distribution of grey levels in the image
Massively useful in image processing, especially in segmentation.

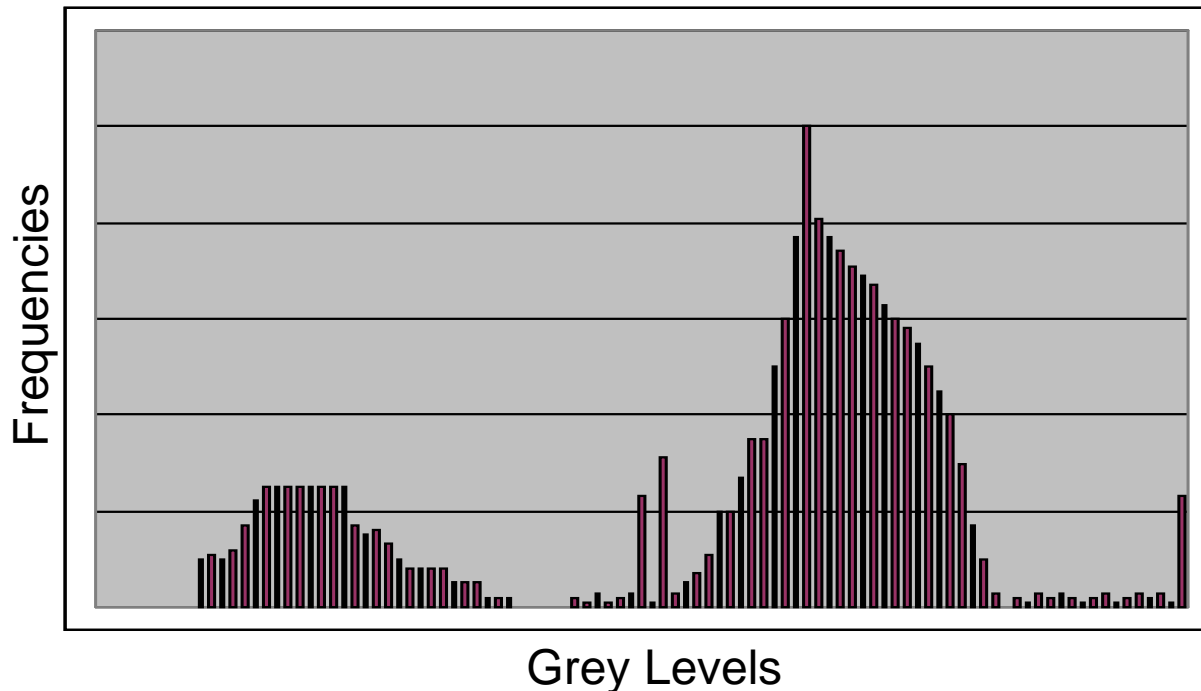


Image Histograms

Histograms plots how many times (frequency) each intensity value in image occurs

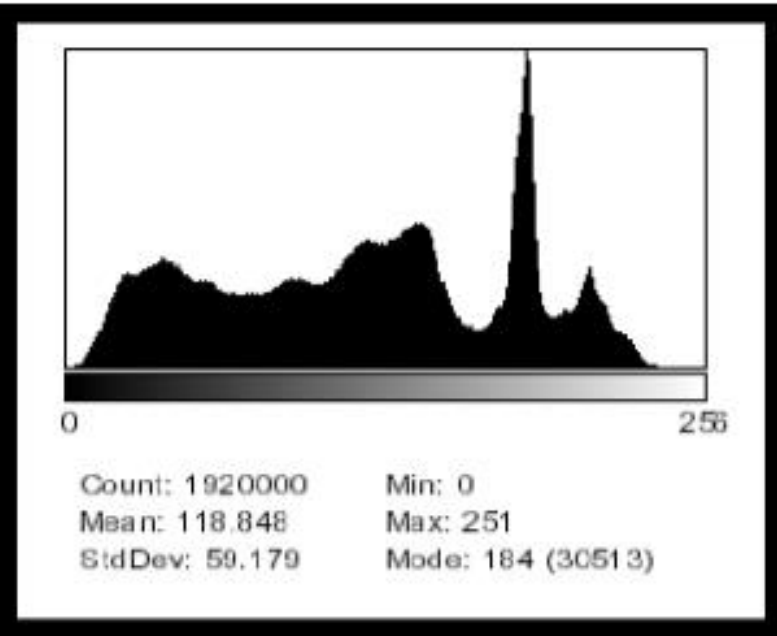
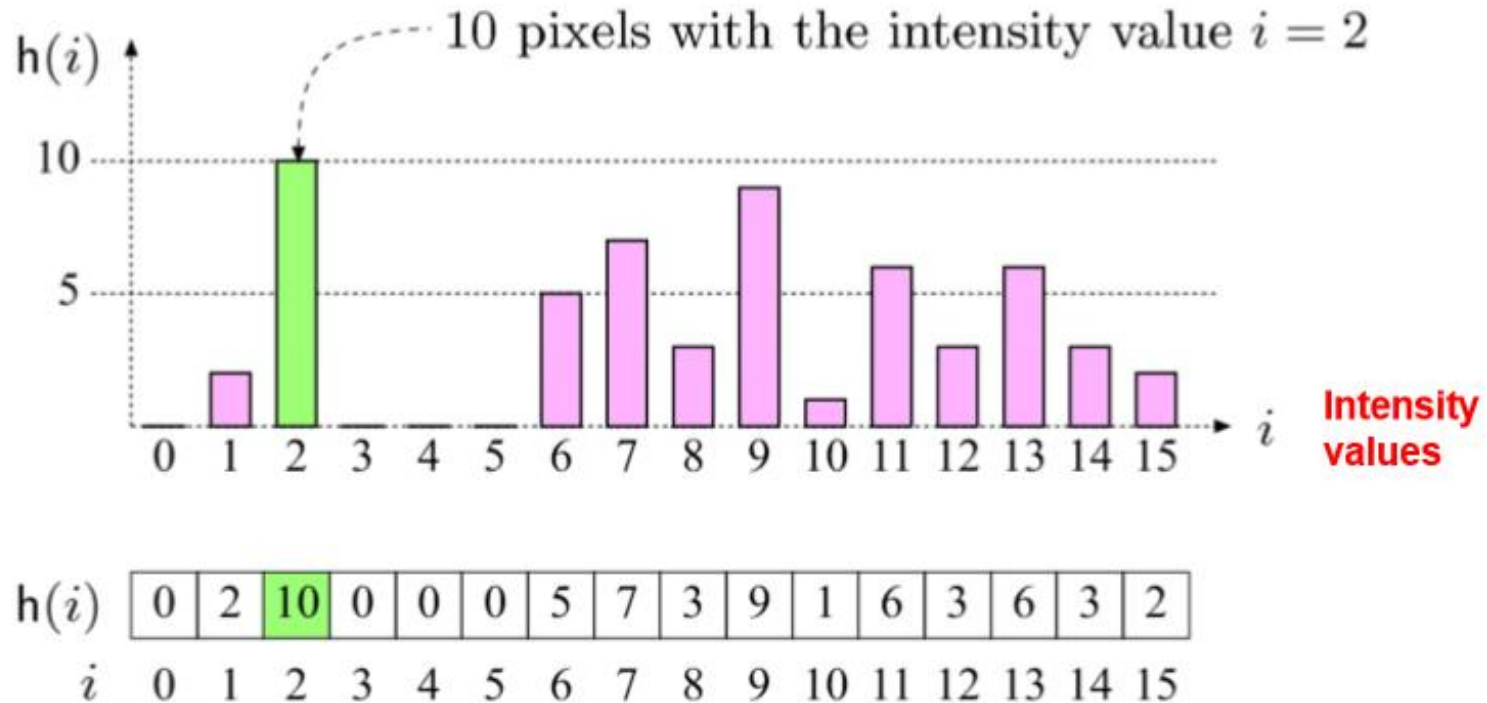


Image Histograms

- Many cameras display real time histogram of a scene.
- Also easier to detect types of processing previously applied to image



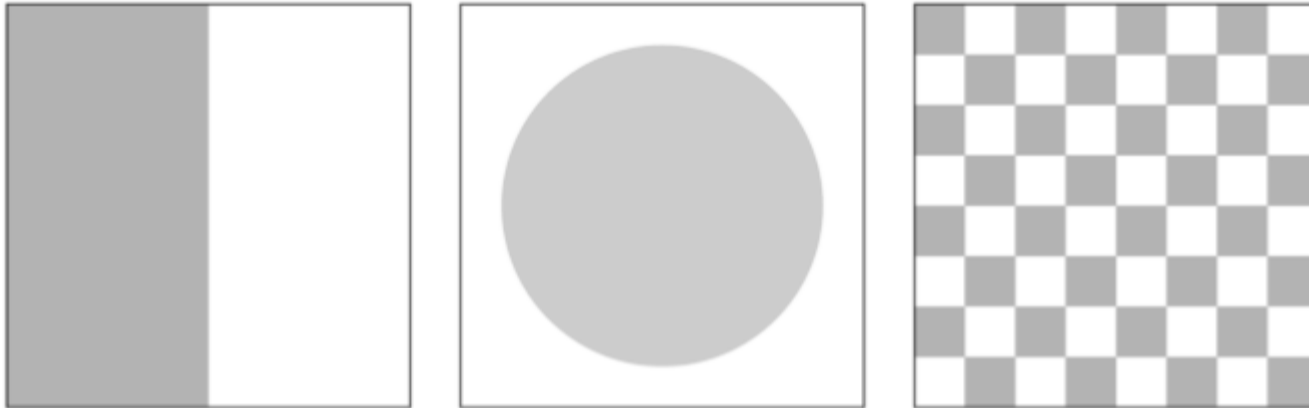
Image Histograms



- Histograms: only statistical information
- No indication of pixels locations

Image Histograms

- Different images can have same histogram
- 3 images below have same histogram



- Half of pixels are gray, half are white
 - Same histogram = same statistics
 - Distribution of intensities could be different
- Can we reconstruct image from histogram?

NO

The histogram of a digital image with gray levels in the range $[0, L-1]$ is a discrete function

$$h(r_k) = n_k$$

r_k : the k th gray level

n_k : the number of pixels in the image having gray level r_k

Dividing each of its values by the total number of pixels in the image (n).

$$p(r_k) = n_k / n$$

For $k = 0, 1, \dots, L-1$.

$p(r_k)$: Gives an estimate of the probability of occurrence of gray level r_k .

The sum of all components of a normalized histogram is equal to 1.

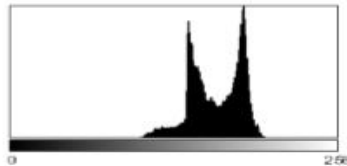
The contrast of a grayscale image indicates how easily objects in the image can be distinguished

- **High contrast image:** many distinct intensity values.
- **Low contrast:** image uses few intensity values.

Histograms and Contrast

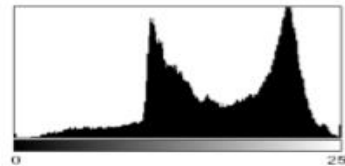
Good Contrast?

Widely spread intensity values + large difference between min and max intensity values



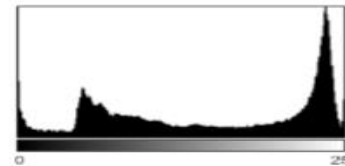
(a)

Low contrast



(b)

Normal contrast



(c)

High contrast

Image

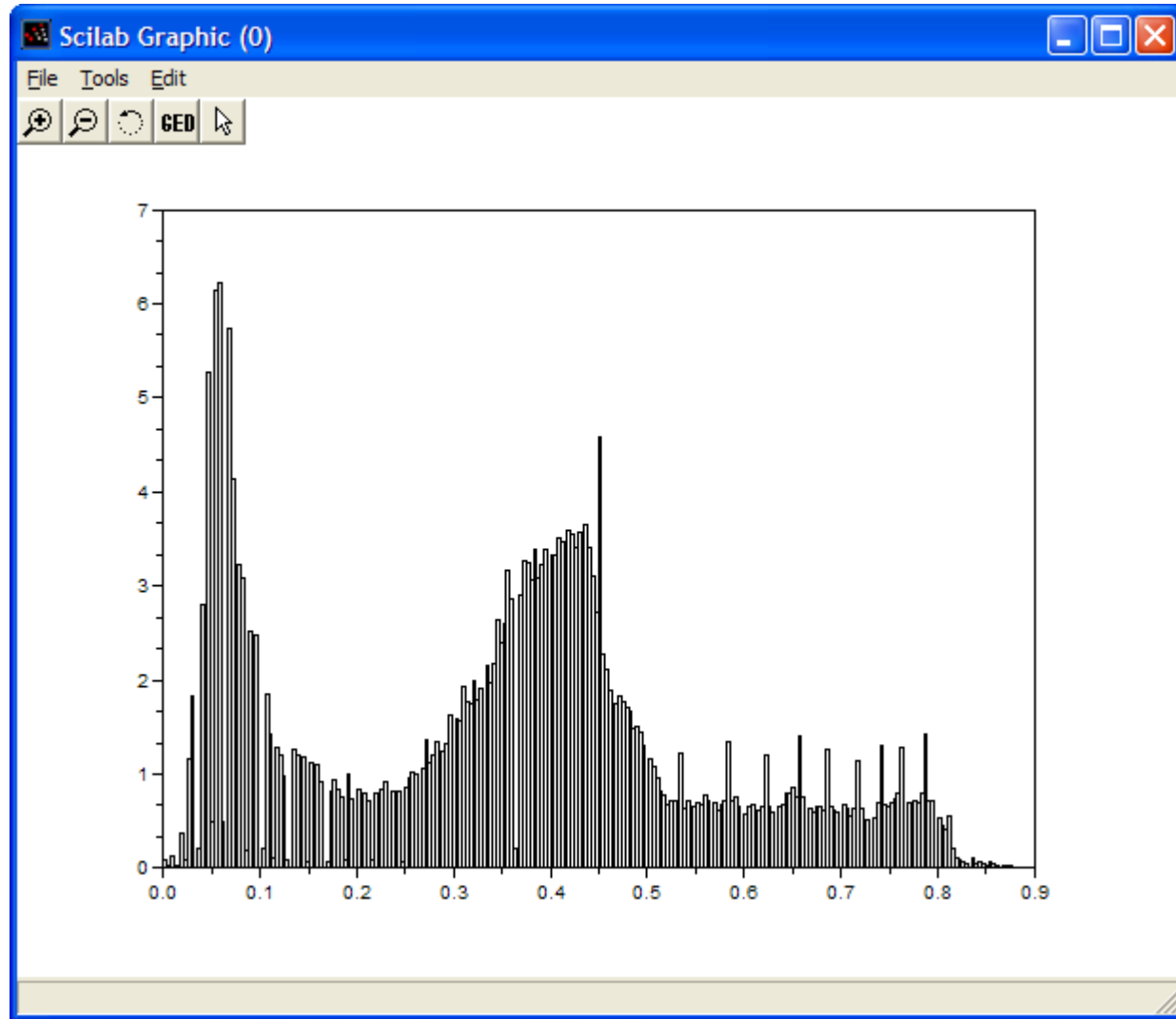
Histogram

Histogram Examples

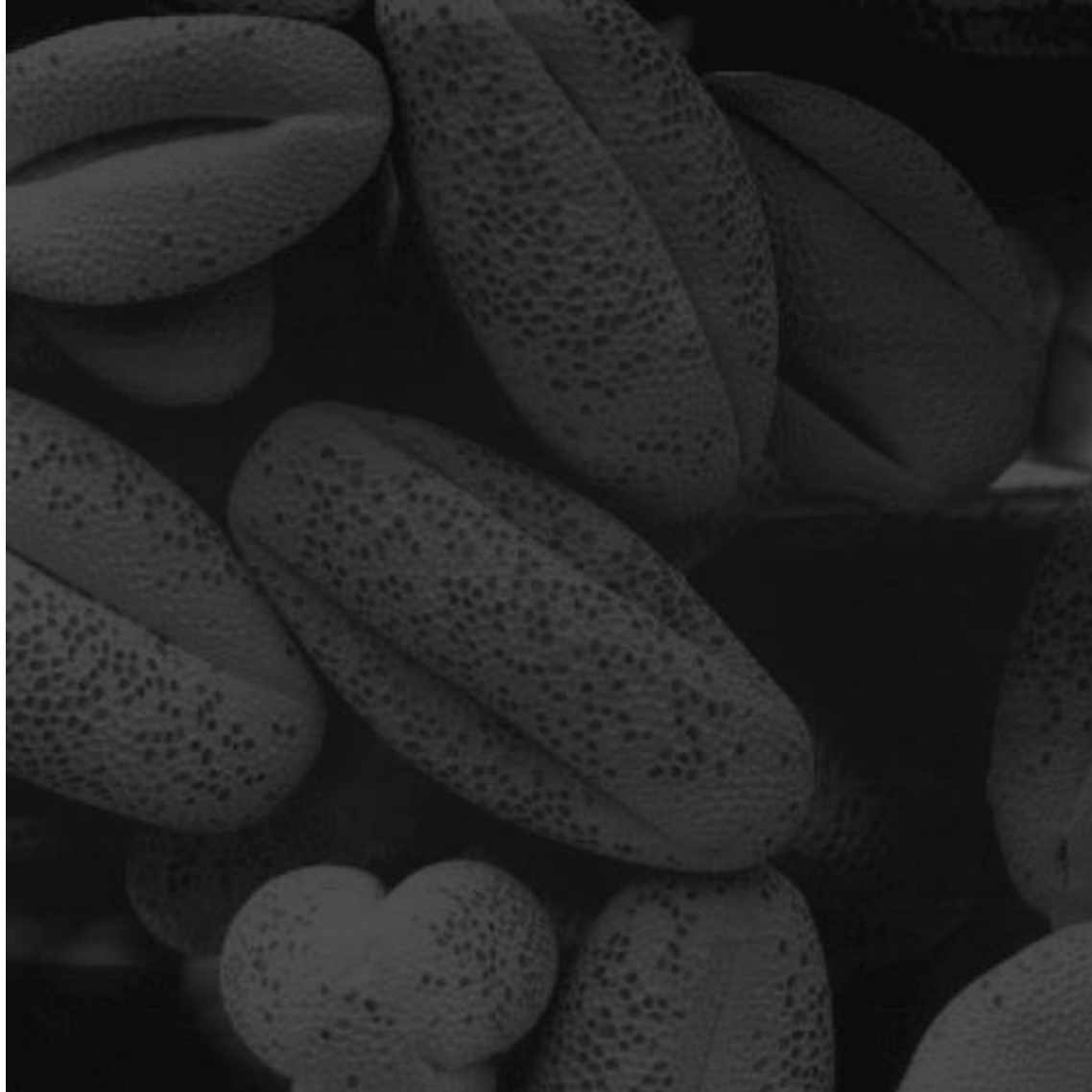


Histogram Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

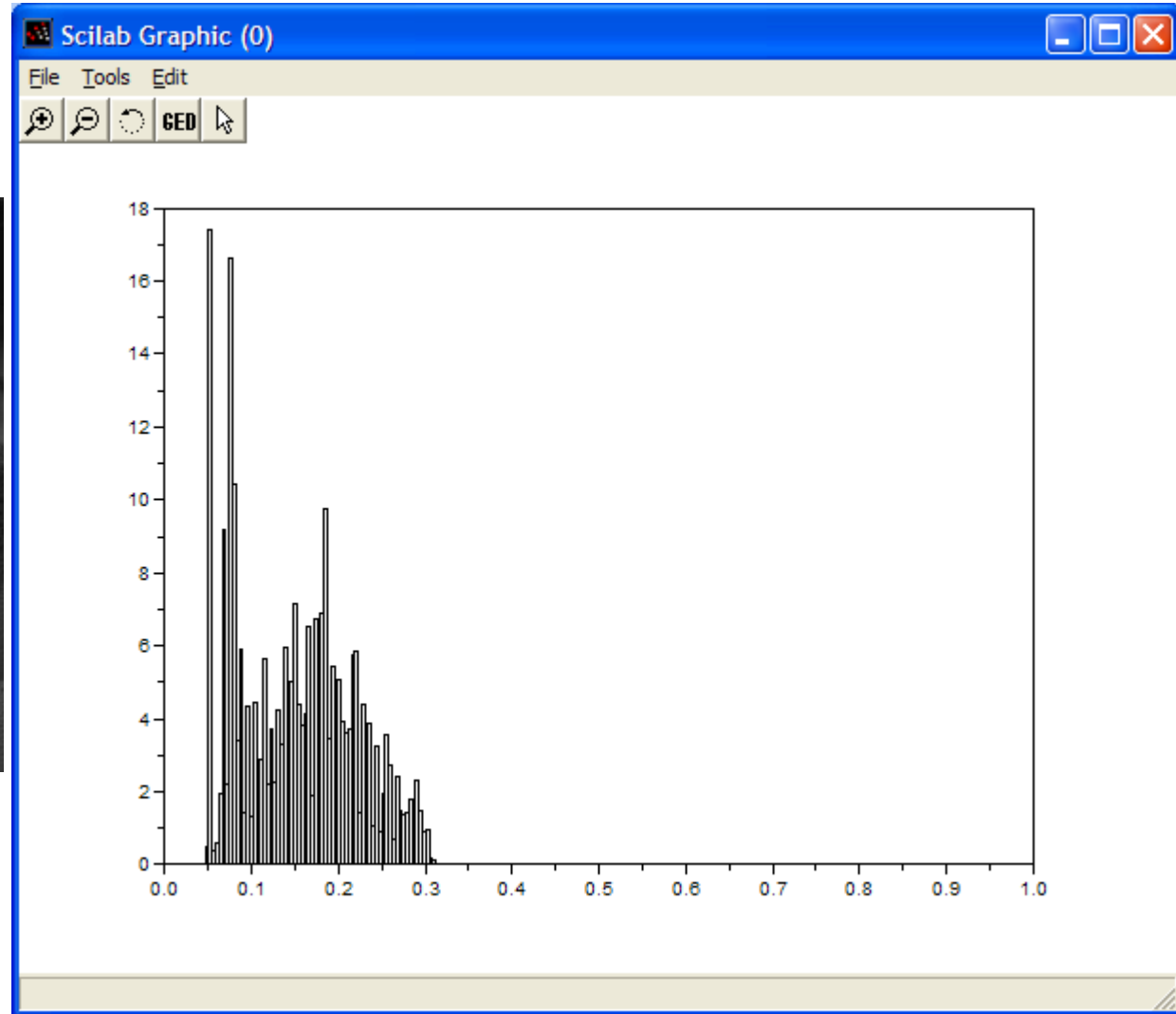
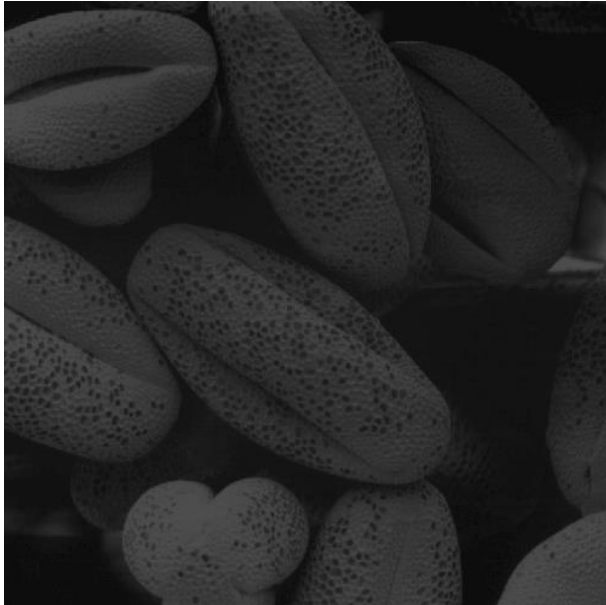


Histogram Examples (cont...)



Histogram Examples (cont...)

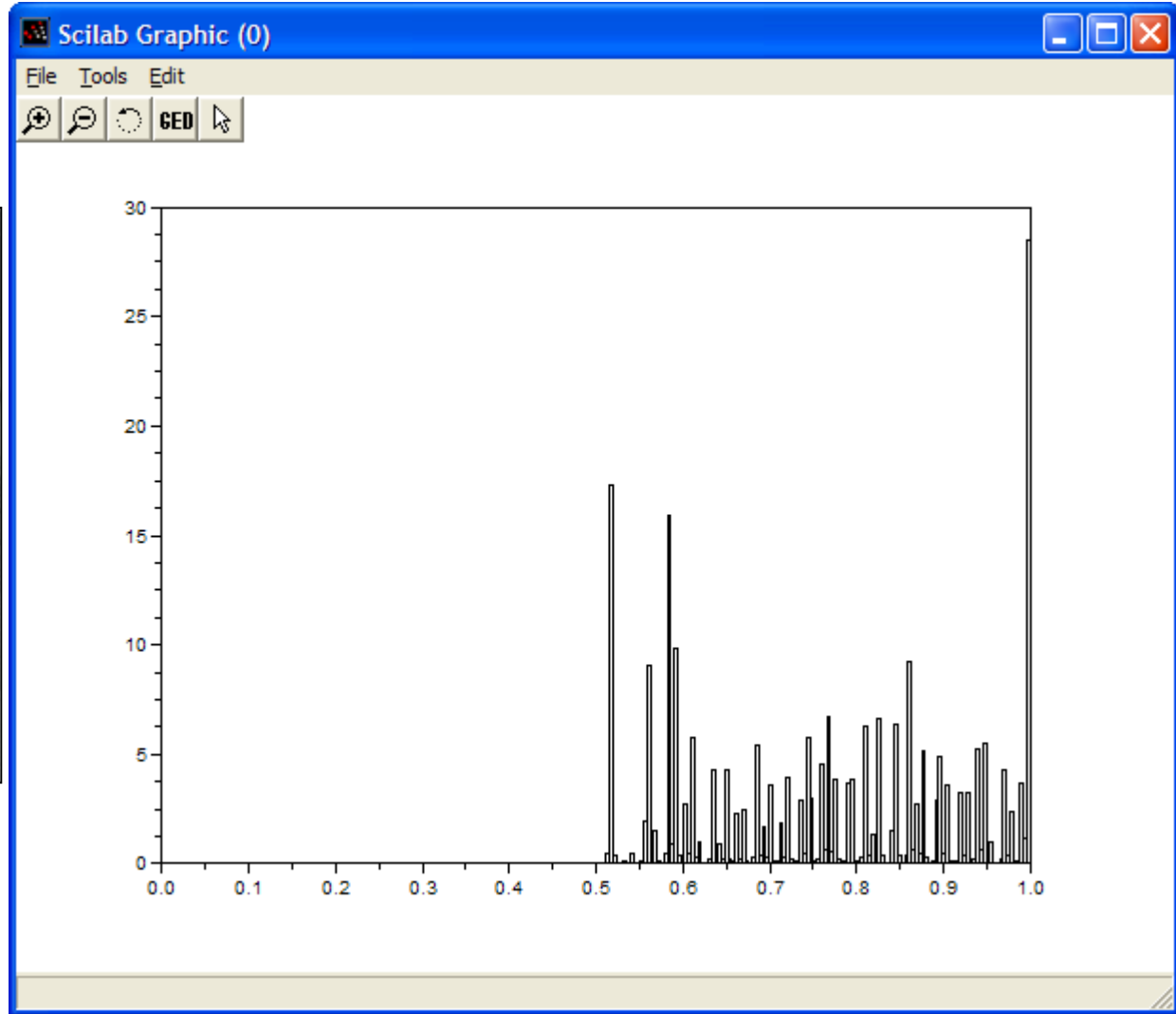
Images taken from Gonzalez & Woods, Digital Image Processing (2002)



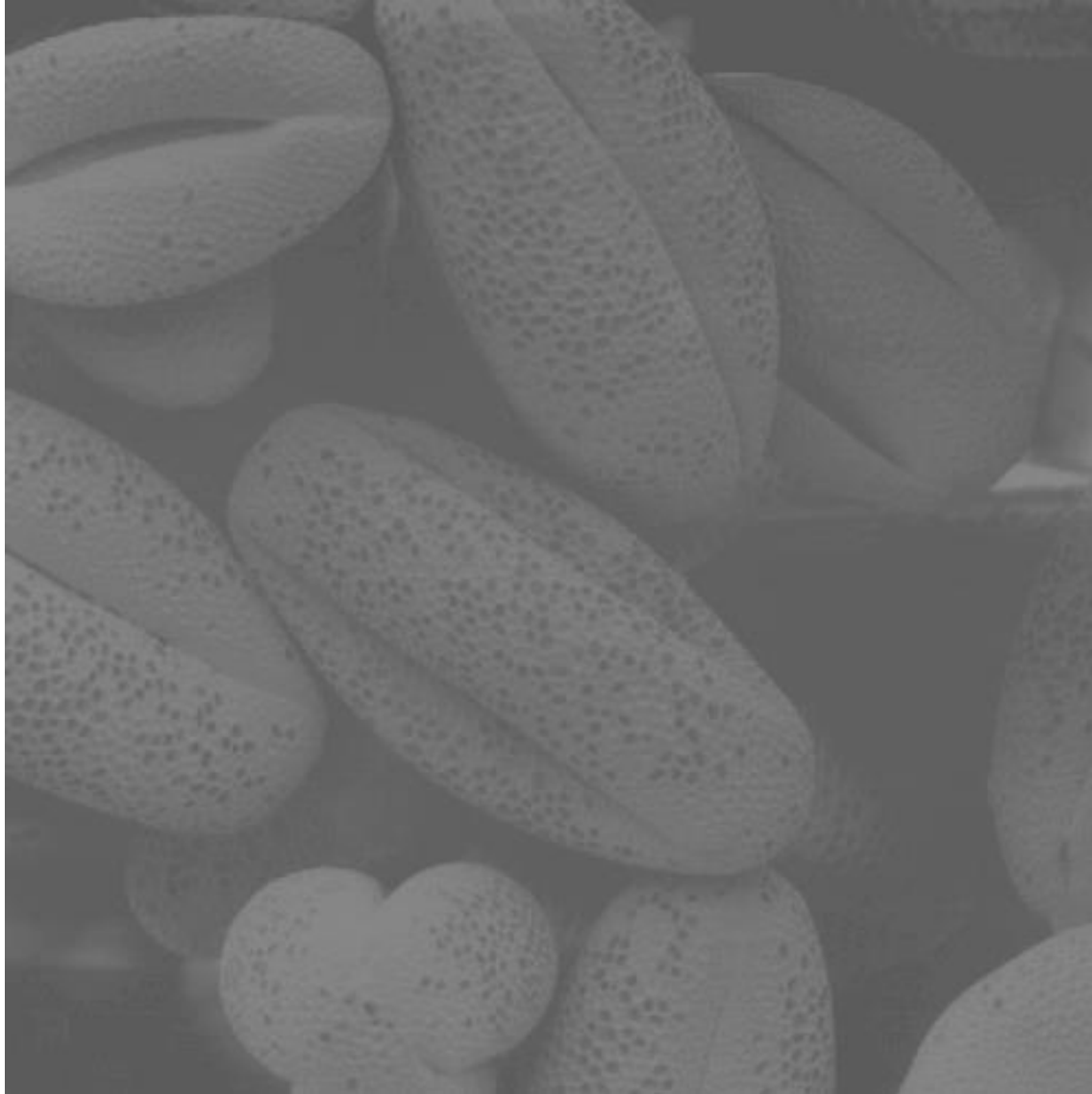
Histogram Examples (cont...)



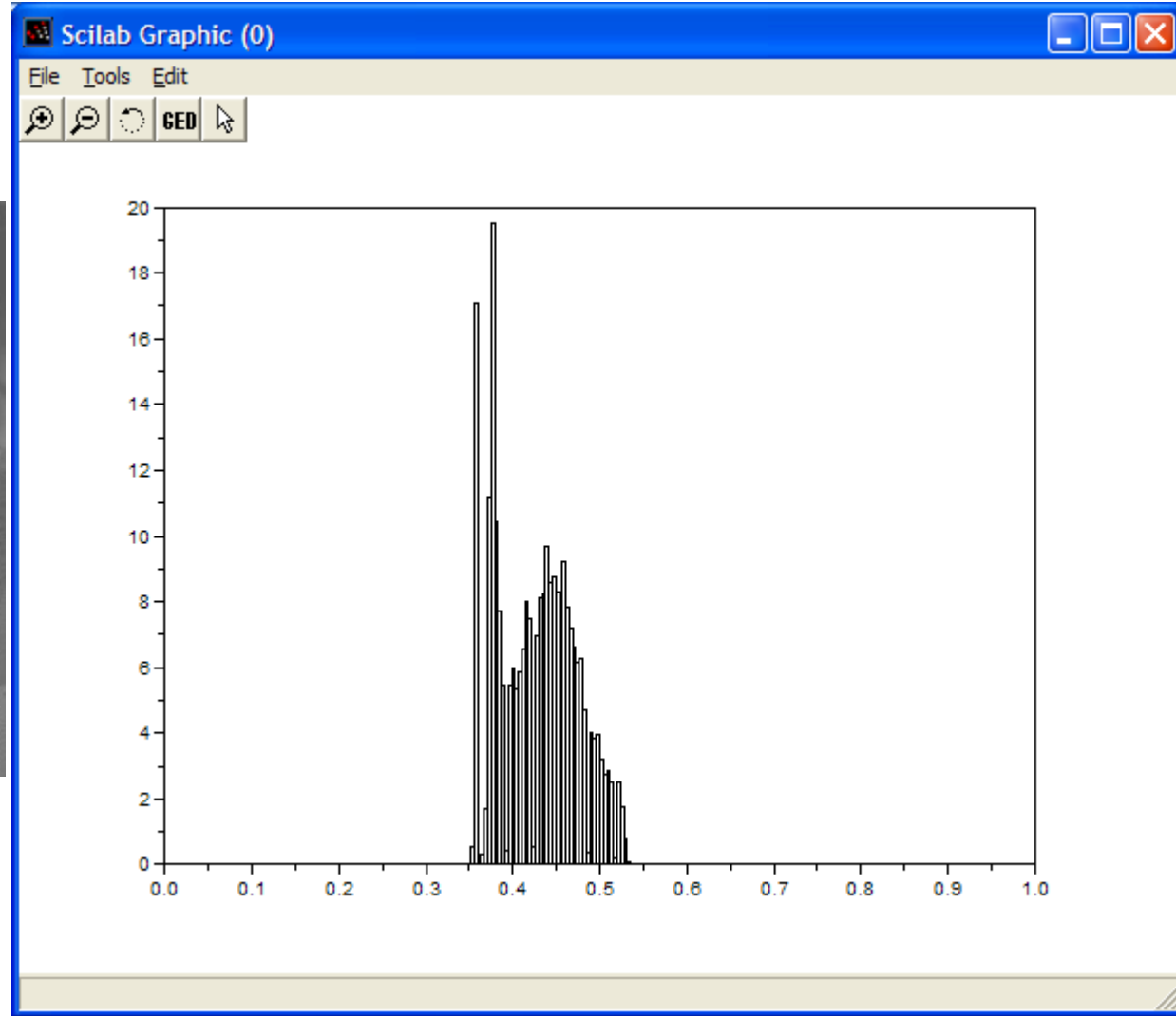
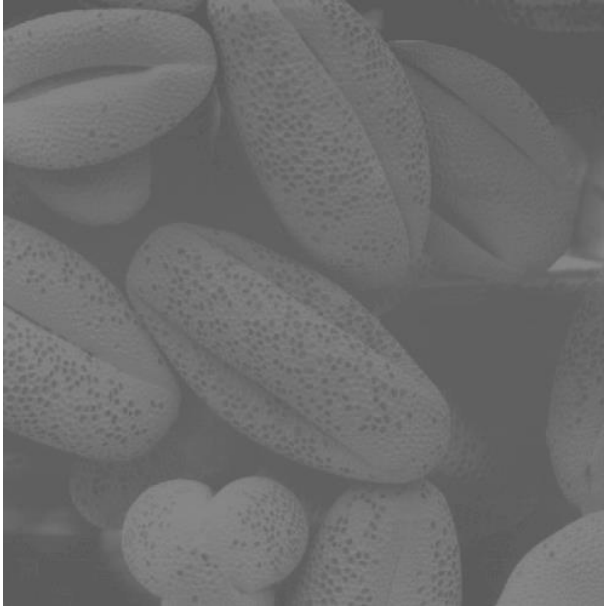
Histogram Examples (cont...)



Histogram Examples (cont...)



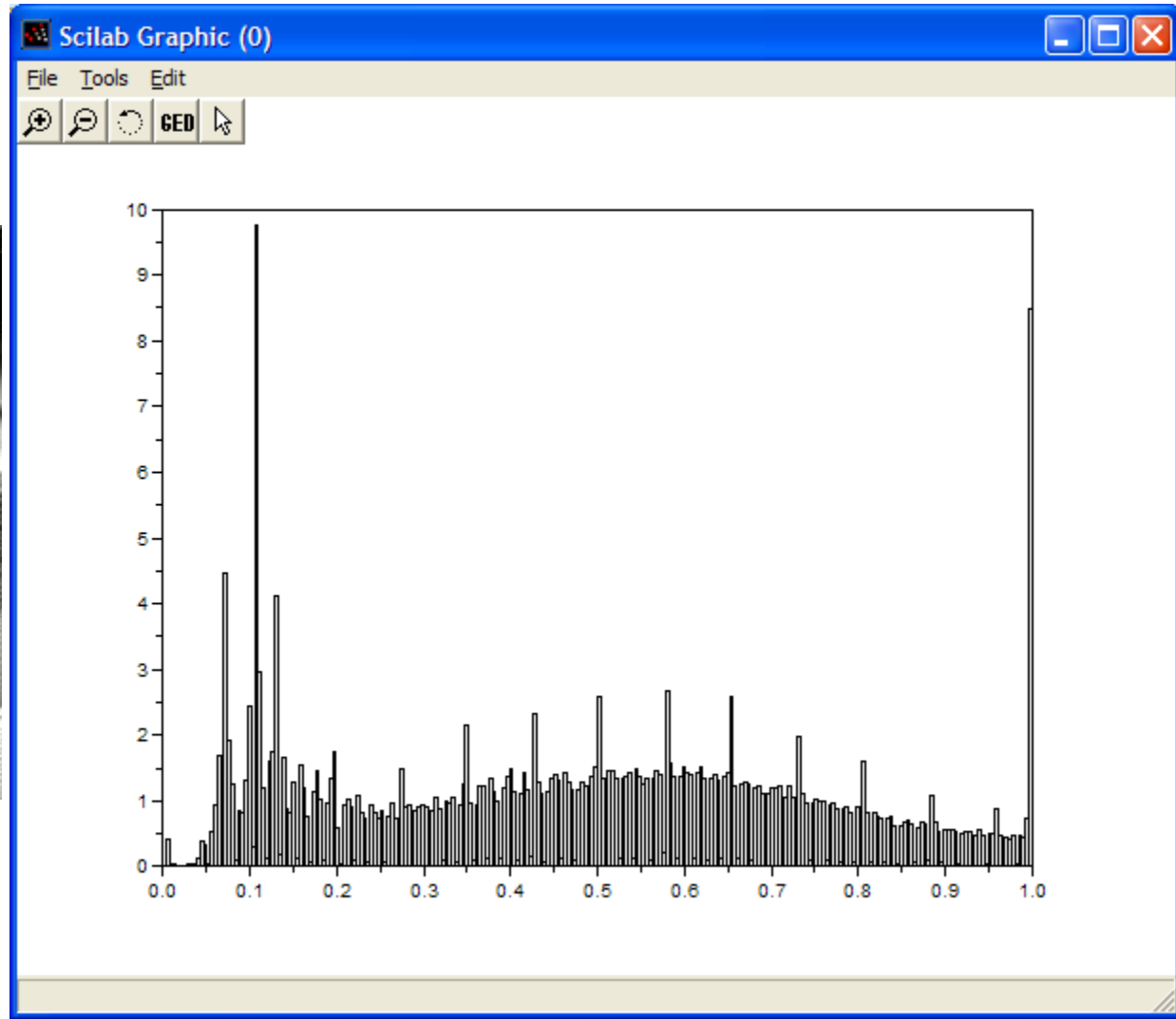
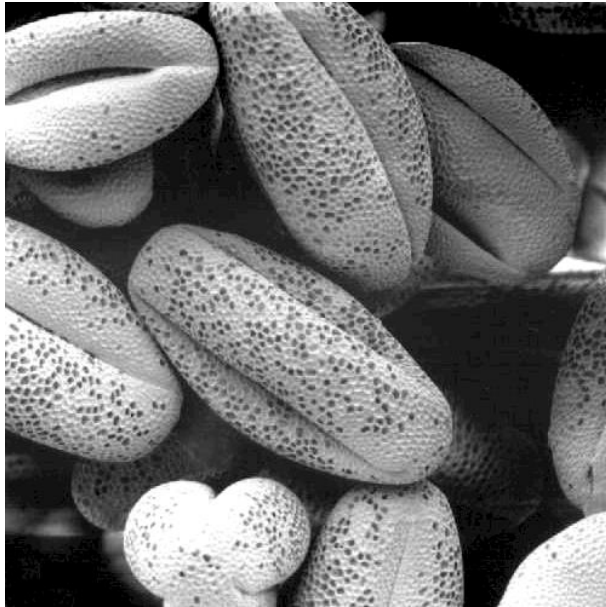
Histogram Examples (cont...)



Histogram Examples (cont...)



Histogram Examples (cont...)

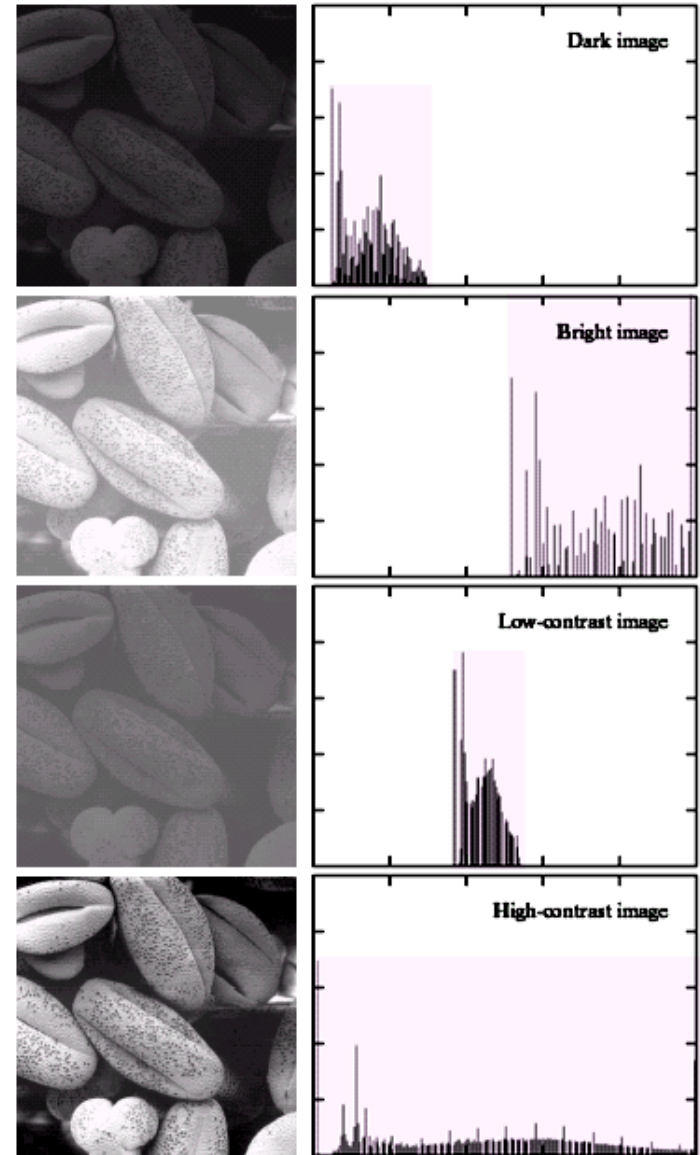


Histogram Examples (cont...)

A selection of images and their histograms

Notice the relationships between the images and their histograms

Note that the high contrast image has the most evenly spaced histogram



Contrast Stretching

We can fix images that have poor contrast by applying a pretty simple contrast specification

The interesting part is how do we decide on this transformation function?



Histogram Equalisation

Spreading out the frequencies in an image (or equalising the image) is a simple way to improve dark or washed out images

Can be expressed as a transformation of histogram

$$s_k = T(r_k)$$

Where:

- r_k : input intensity
- s_k : processed intensity
- k : the intensity range
(e.g 0.0 – 1.0)

Histogram Equalisation

Let the variable r represent the gray levels of the image to be enhanced, with $r=0$ representing black and $r=1$ representing white.

For any r , the following transformations produce a level s for every pixel value r in the original image.

$$s = T(r) \quad 0 \leq r \leq 1$$

The transformation function $T(r)$ satisfies the following condition:

- (a) $T(r)$ is a single-valued and monotonically increasing in the interval $0 \leq r \leq 1$
- (b) $0 \leq T(r) \leq 1$ for $0 \leq r \leq 1$

Histogram Equalisation

- The requirement in (a) that $T(r)$ be single valued is needed to guarantee that the inverse transformation will exist, and monotonicity condition preserves the increasing order from black to white in the output image.
- i.e. A pixel which is darker in the original image should remain darker in the processed image, and a pixel which is brighter in the original should remain brighter in the processed image.

Histogram Equalisation

- Condition (b) guarantees that the output gray levels will be in the same range as the input levels.
- i.e. Ensure that the processed image that you get doesn't lead to a pixel value which is higher than the max. intensity value that is allowed.

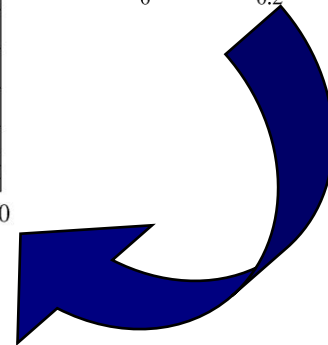
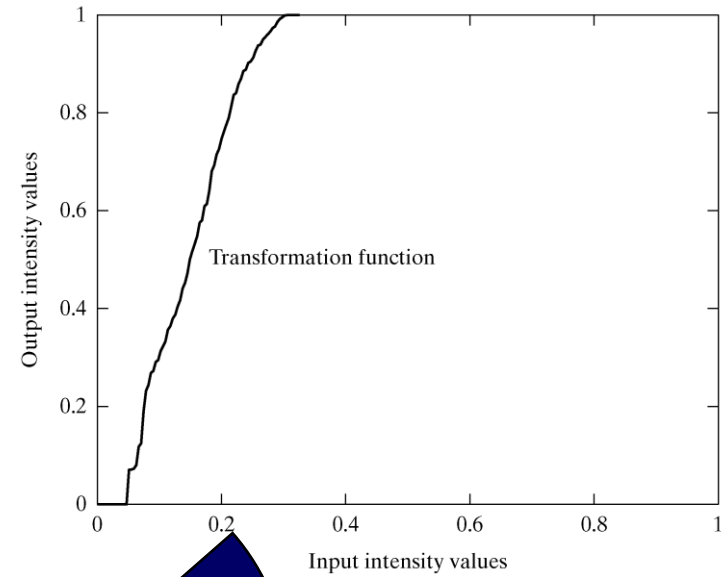
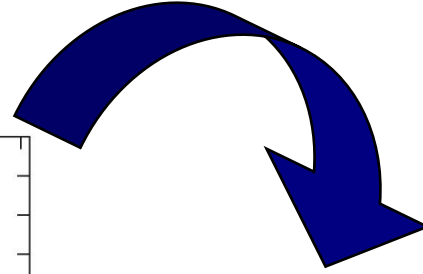
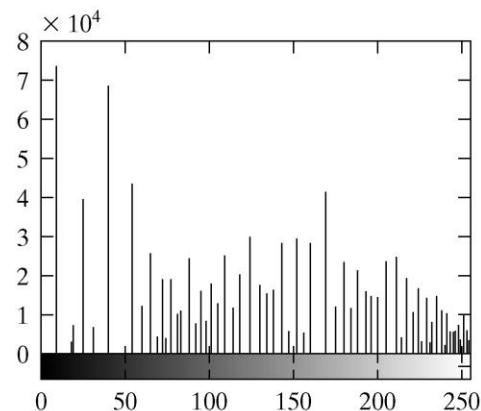
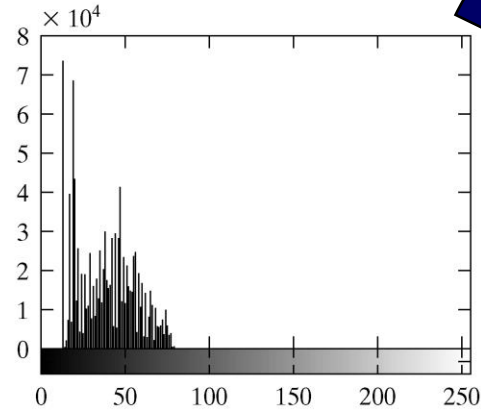
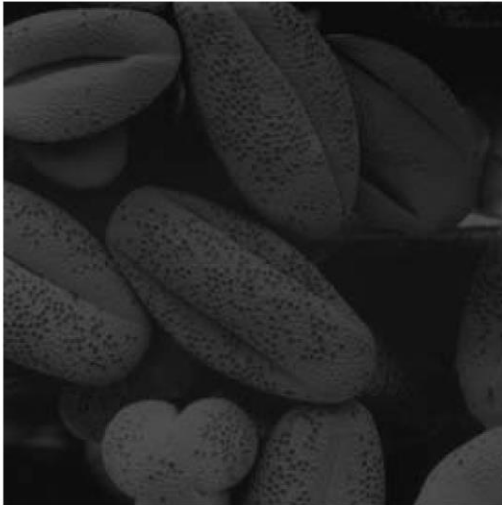
The formula for histogram equalisation is given where

- r_k : input intensity
- s_k : processed intensity
- k : the intensity range
(e.g 0.0 – 1.0)
- n_j : the frequency of intensity j
- n : the sum of all frequencies

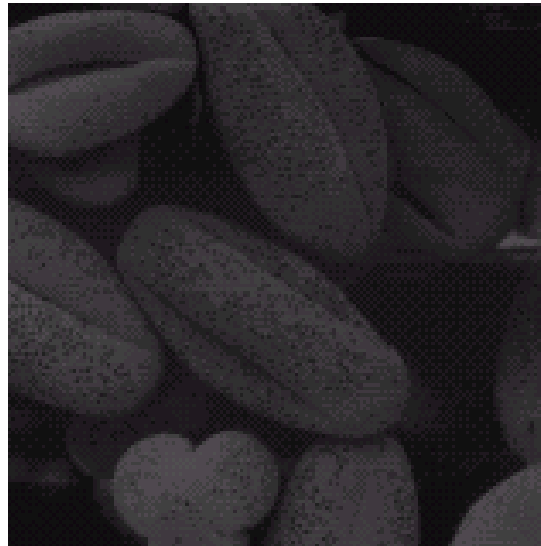
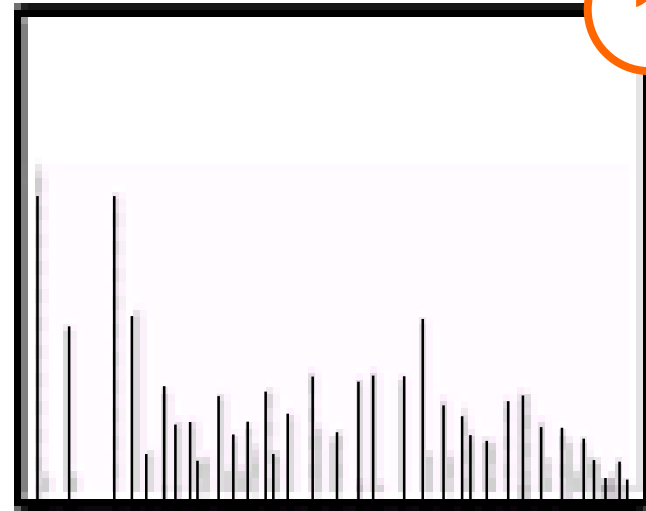
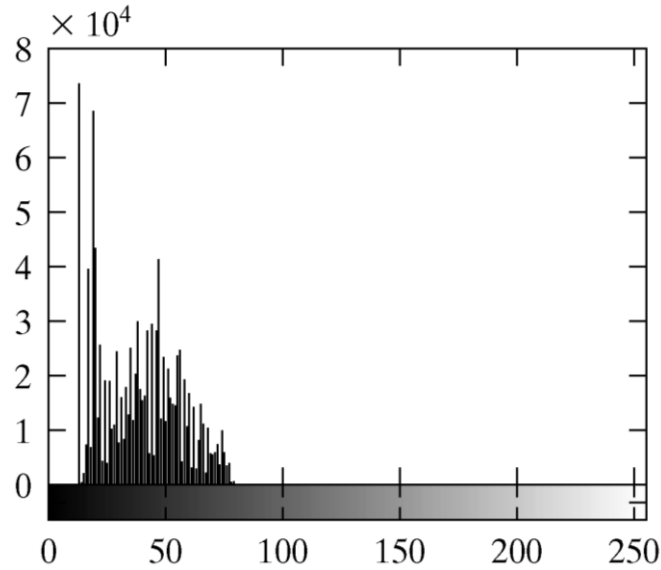
$$\begin{aligned} s_k &= T(r_k) \\ &= \sum_{j=1}^k p_r(r_j) \\ &= \sum_{j=1}^k \frac{n_j}{n} \end{aligned}$$

Equalisation Transformation Function

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

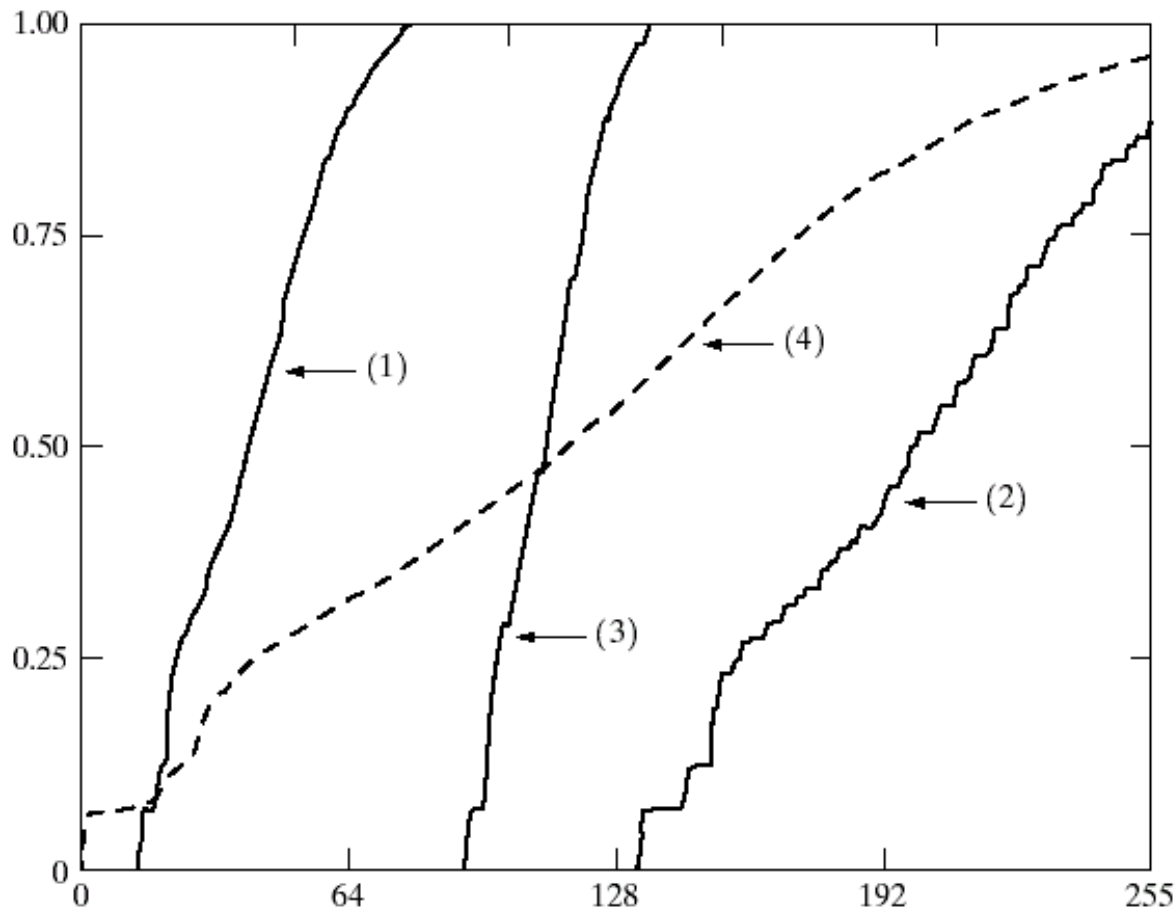


Equalisation Examples



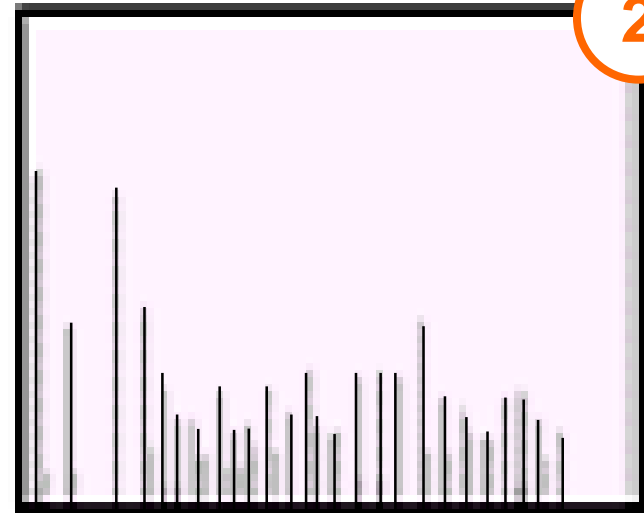
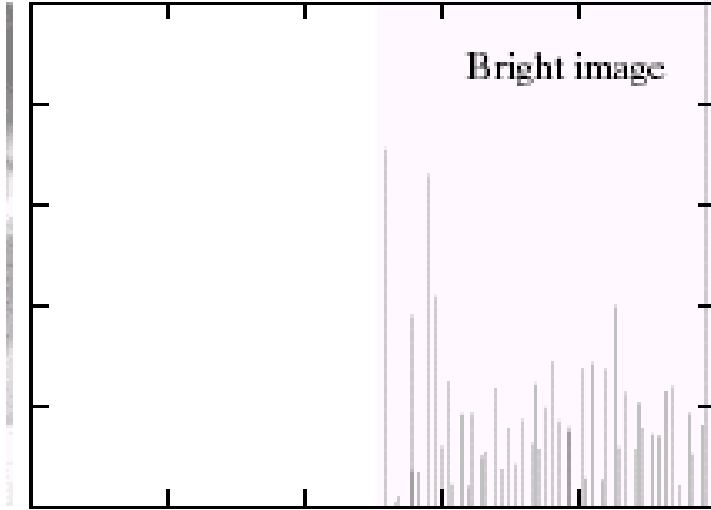
Equalisation Transformation Functions

The functions used to equalise the images in the previous example



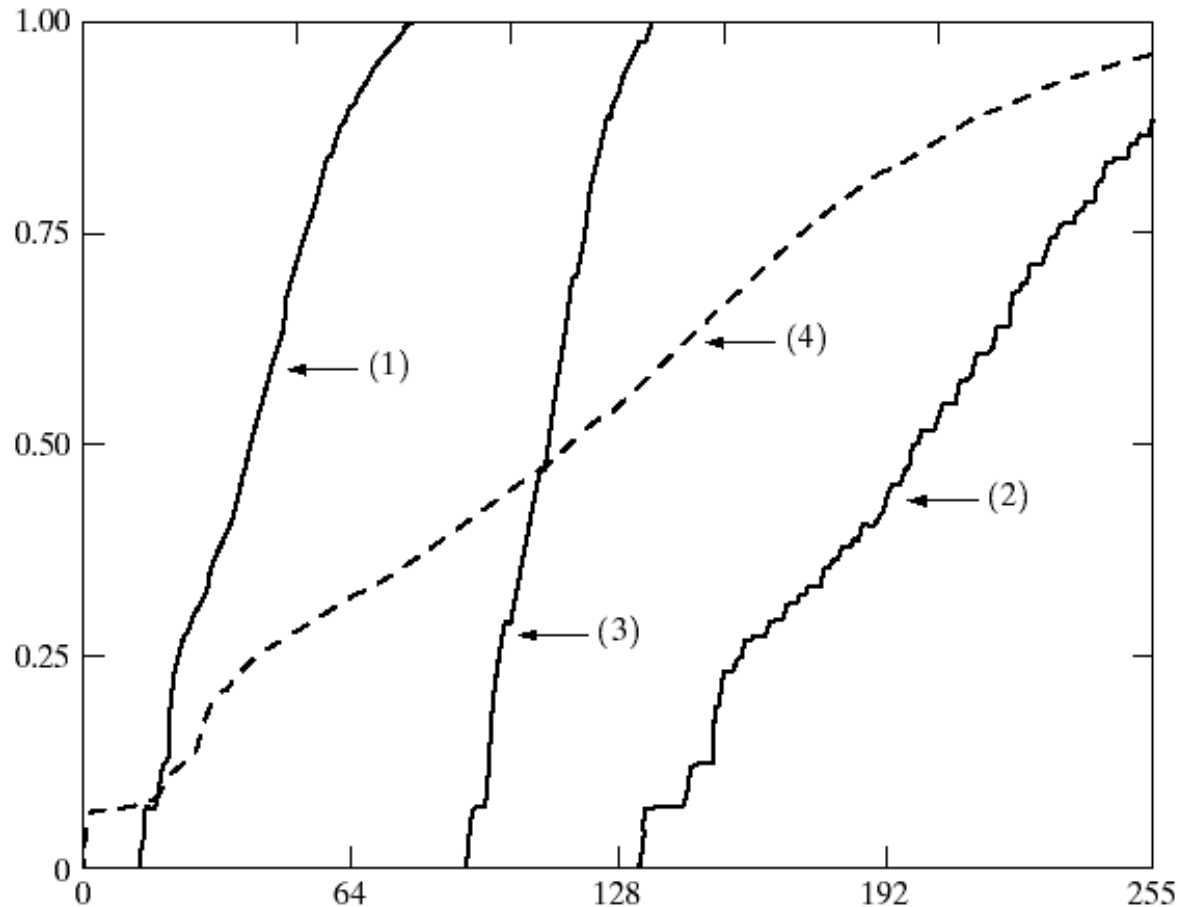
Equalisation Examples

2



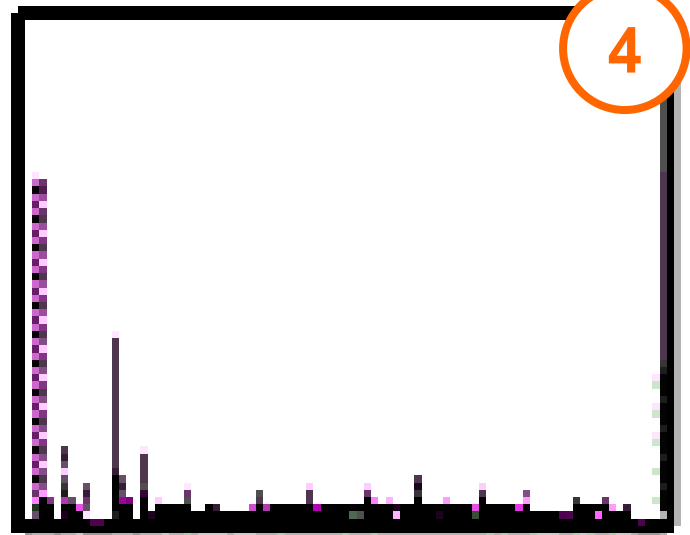
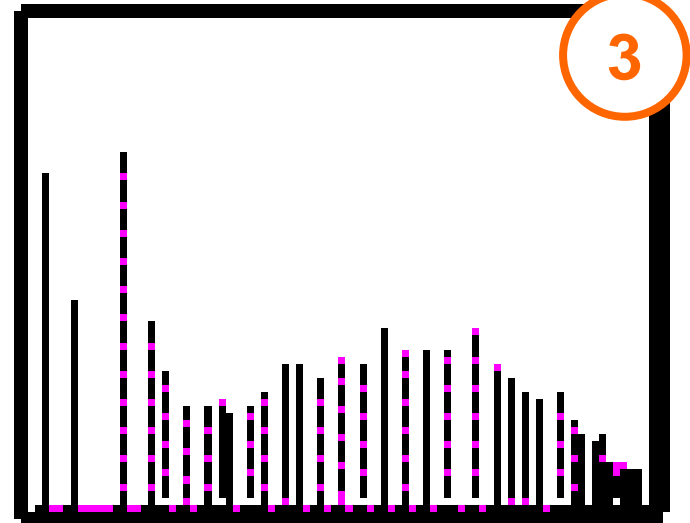
Equalisation Transformation Functions

The functions used to equalise the images in the previous example

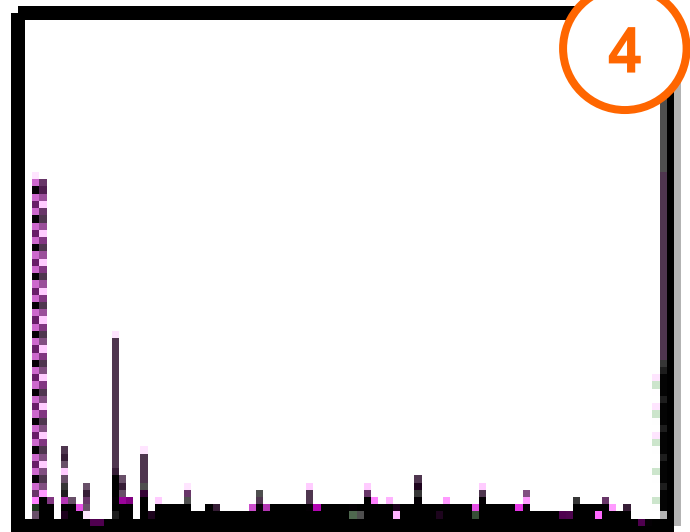
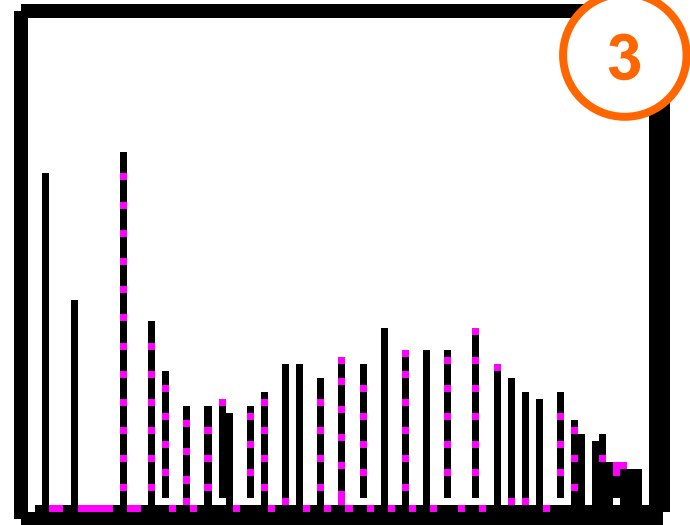


Equalisation Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

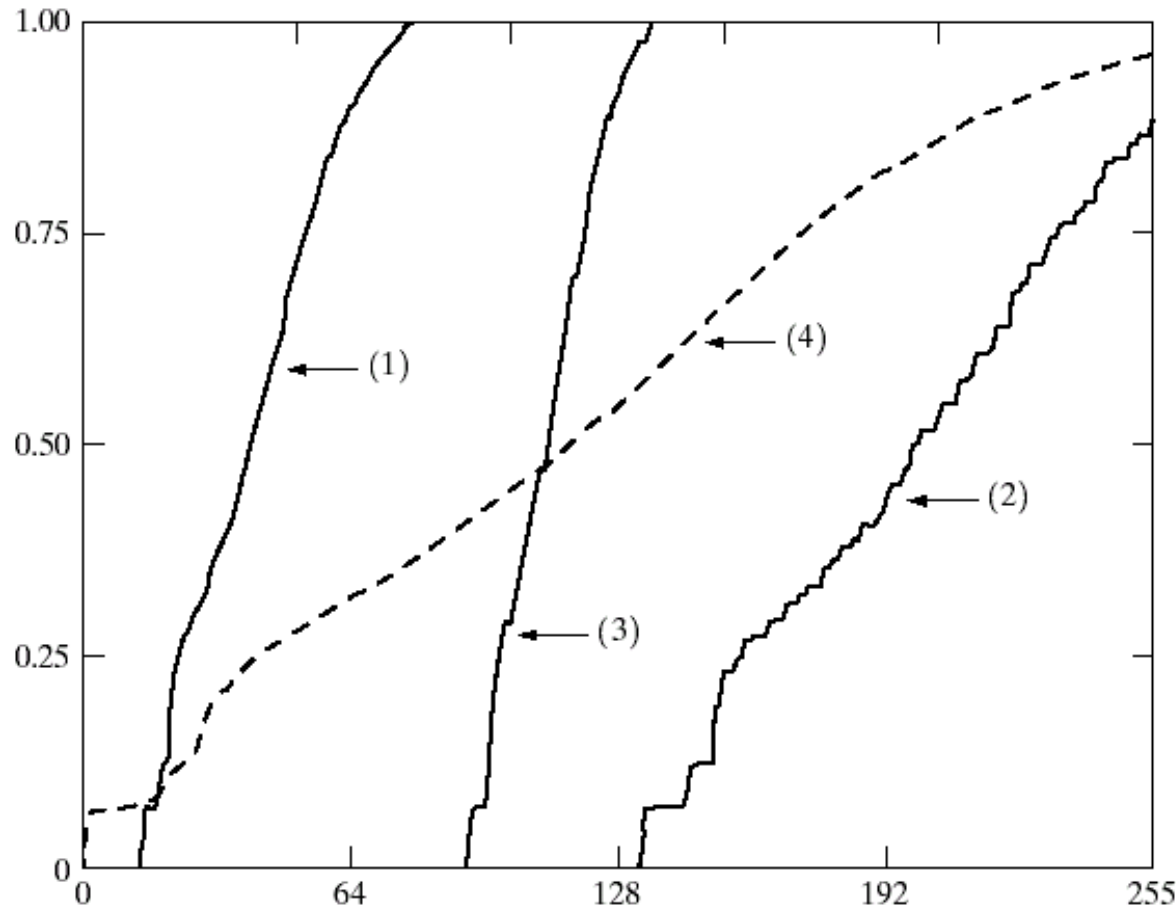


Equalisation Examples (cont...)



Equalisation Transformation Functions

The functions used to equalise the images in the previous examples



1. Histogram equalization proof.

2. Exposure?

- a. Underexposed
- b. Properly Exposed
- c. Overexposed

We have looked at:

- Different kinds of image enhancement
- Histograms
- Histogram equalisation

Next time we will start to look at point processing and some neighbourhood operations